HW#4

Assigned: Thursday, September 17, 2009

Due: Thursday, October 1, 2009

We derived the shape factor using Finite Difference method for a 2-D problem. Now using either F.D or the equation below:

$$\sigma = \frac{1}{V_i} \sum_{i=1}^n \frac{A_i}{d_i}$$
 (Kazemi-Gilman, 1990)

Where

V: Volume of the matrix block

A: Area of a surface open to flow in a given flow direction

d: distance from the open surface to the center of the matrix block

n: number of faces

 Σ : Summation over all open surfaces of a matrix block

Part a) Show that for a cylindrical matrix block: $\sigma = \frac{8}{d^2}$

Part b) Show that for a spherical matrix block: $\sigma = \frac{12}{d^2}$

Part c)

Derive the shape factor for the 2D homogeneous anisotropic case using the finite difference method. Use the following coordinate transformation:

$$(x,y) \to \left(\overline{X},\overline{Y}\right)$$

where

$$\overline{X} = \frac{x}{\sqrt{k_{xm}}}$$
$$\overline{Y} = \frac{y}{\sqrt{k_{ym}}}$$