

■ **General Calculations**

■ **For Class**

For the Exponential Integral defined by :

$$\text{Ei}[x] = - \int_{-x}^{\infty} \frac{\text{Exp}[-u]}{u} du$$

For desired precision ϵ (for example 10^{-6} , 10^{-10} , 10^{-20})

If $x < \text{Abs}[\text{Ln}[\epsilon]]$, use

$$\gamma + \text{Ln}[x] + \sum_{n=1}^{\infty} \frac{x^n}{n * n!} \text{ until } \frac{x^n}{n * n!} < \epsilon$$

If $x \geq \text{Abs}[\text{Ln}[\epsilon]]$

$$\frac{\text{Exp}[x]}{x} \left(\sum_{n=1}^{\infty} \frac{n!}{x^n} \text{ until } \frac{n!}{x^n} < \epsilon \right)$$

Where γ is Euler's constant:

N[EulerGamma, 100]

0.5772156649015328606065120900824024310421593359399235988057672348848677267776646709369470 :
632917467495