Identifying quantitative trait loci via group-sparse multitask regression and feature selection: an imaging genetics study of the ADNI cohort

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ABSTRACT

Motivation: Recent advances in high-throughput genotyping and brain imaging techniques enable new approaches to study the influence of genetic variation on brain structures and functions. Traditional association studies typically employ independent and pairwise univariate analysis, which treats single nucleotide polymorphisms (SNPs) and quantitative traits (QTs) as isolated units and ignores important underlying interacting relationships between the units. New methods are proposed here to overcome this limitation.

Results: Taking into account the interlinked structure within and between SNPs and imaging QTs, we propose a novel Group-Sparse Multi-task Regression and Feature Selection (G-SMuRFS) method to identify quantitative trait loci for multiple disease-relevant QTs and apply it to a study in mild cognitive impairment and Alzheimer’s disease. Built upon regression analysis, our model uses a new form of regularization, group ℓ1,2-norm (Gℓ1,2-norm), to incorporate the biological group structures among SNPs induced from their genetic arrangement. The new Gℓ1,2-norm considers the regression coefficients of all the SNPs in each group with respect to all the QTs together and enforces sparsity at the group level. In addition, an ℓ2,1-norm regularization is utilized to couple feature selection across multiple tasks to make use of the shared underlying mechanism among different brain regions. The effectiveness of the proposed method is demonstrated by both clearly improved prediction performance in empirical evaluations and a compact set of selected SNP predictors relevant to the imaging QTs.

Availability: Software is publicly available at: http://ranger.uta.edu/ %7eheng/ imaging-genetics/

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Supplementary information: Supplementary data are available at Bioinformatics online.

1 INTRODUCTION

Imaging genetics is an emergent transdisciplinary research field, where the associations between genetic variations and imaging measures as quantitative traits (QTs) or continuous phenotypes are evaluated. Compared to case–control status, the QTs have increased statistical power and are closer to the underlying biological etiology of the disease making it easier to identify underlying genes (Braskie et al., 2011; Potkin et al., 2009; Shen et al., 2010; Stein et al., 2010; Yip and Lange, 2011; Zhan et al., 2011). Genome-wide association studies (GWAS) have been increasingly performed to correlate high-throughput single nucleotide polymorphism (SNP) data to large-scale image data. While many studies employed a hypothesis-driven approach by making significant reduction in one or both data types (Bralten et al., 2011), some recent studies examined these associations at the whole genome entire brain level (Shen et al., 2014; Stein et al., 2014). Pairwise univariate analysis was typically used in traditional association studies to quickly provide important association information between SNPs and QTs. However, it treated the SNPs and the QTs as independent and isolated units, and therefore the underlying interacting relationships between the units might be lost. Multivariate methods to examine joint effect of multi-locus genotype on a single phenotype were studied in general genetic association studies (Bralten et al., 2011; Wu et al., 2007) as well as several recent imaging genetic studies (Bralten et al., 2011; Hobar et al., 2011). This paradigm did not consider the relationship between interlinked brain phenotypes and thus still had limited power in revealing complex imaging genetic associations. In this work, taking into account the interrelated structure within and between SNPs and QTs, we propose a new framework for effectively identifying quantitative trait loci, which addresses the following challenges in imaging genetics association study.

First, traditional association studies consider all the SNPs evenly distributed and assess each SNP individually. However, certain SNPs are naturally connected via different pathways. Multiple SNPs from one gene often jointly carry out genetic functionalities. Moreover,
The latter is important because in reality only a small fraction \( \ell \), in which the coefficients of the SNPs within a regularization feature selection becomes an integrated procedure across multiple removed. Lastly, through enforcing of genotypes are related to a specific phenotype. Moreover, \( \ell \) of treating SNPs in an isolated manner, it would be beneficial to exploit the group structure among SNPs.

Second, because the functionality of the human brain typically involves more than one cerebral component, investigating each individual regional brain phenotype separately will inevitably lose the interacting relationships between them. For example, the brain’s episodic memory network, including medial temporal lobe (MTL) structures, medial and lateral parietal, and prefrontal cortical areas, are normally engaged together during episodic recall (Waltzoff et al., 2011). In addition, accurate prediction of disease status and progression are typically implicated by multiple brain regions coupled with other biomarkers (Rancati et al., 2010) Therefore, jointly analyzing all the imaging phenotypes via one single integral regression model is desirable to elucidate the shared mechanism that may be hidden otherwise.

By recognizing the interrelated nature of these genotypes and phenotypes, in this study, we propose a novel Group-Sparse Multi-task Regression and Feature Selection (G-SMuRFS) method to identify quantitative trait loci in a mild cognitive impairment (MCI) and Alzheimer’s disease (AD) study using a few important imaging QTs relevant to AD. We consider each SNP as a feature in each QT as a response variable (i.e. a learning task), and formulate a multitask regression framework including multiple features (SNPs) and multiple responses (QTs). Our goal is to reveal the relationships between these genetic features and imaging phenotypes.

The proposed model consists of three major components. First, it is built upon regression analysis due to the continuous responses of the imaging phenotypes. As a result, the regression coefficients assess the relationships between SNPs and QTs. Second, in order to address the group-wise association among SNPs, inspired by group Lasso (Yuan and Lin, 2006), we propose a new form of regularization, called as group \( \ell_2,1 \)-norm (G\( \ell_2,1 \)-norm) regularization, in which the coefficients of the SNPs within a pre-defined group, with respect to all the QTs, are penalized as a whole via \( \ell_2 \)-norm, while \( \ell_1 \)-norm is used to sum up the group-wise penalties to enforce sparsity between groups (Tibshirani, 1996). The latter is important because in reality only a small fraction of genotypes are related to a specific phenotype. Moreover, with sparsity, outliers and irrelevant associations are inherently removed. Lastly, through enforcing \( \ell_2,1 \)-norm regularization, feature selection becomes an integrated procedure across multiple learning tasks (Avraamidou et al., 2009; Borzoni et al., 2007), such that the interrelationships among different imaging phenotypes are leveraged. Note that the proposed \( \ell_2,1 \)-norm and the enforced \( \ell_2,1 \)-norm couple a set of learning tasks together such that the regression analysis can be carried out jointly across all the QTs, whereas Lasso (Tibshirani, 1996) and group Lasso (Yuan and Lin, 2006) perform regression analysis separately, one task at a time.

We apply the proposed G-SMuRFS method to the Alzheimer’s disease neuroimaging initiative (ADNI) cohort (Weiner et al., 2010) for identifying quantitative trait loci (QTLs) in MCI and AD using a set of imaging phenotypes known to be relevant to AD. Our empirical results yield not only clearly improved prediction performance in all test cases, but also a compact set of SNP predictors relevant to the imaging genotypes that are in accordance with prior studies.

2 MATERIALS AND DATA SOURCES

Both SNP and structural magnetic resonance imaging (MRI) data used in the preparation of this article were obtained from the Alzheimer’s Disease Neuroimaging Initiative (ADNI) database (adni.loni.ucla.edu). One goal of ADNI has been to test whether serial MRI, positron emission tomography (PET), other biological markers, and clinical and neuropsychological assessment can be combined to measure the progression of MCI and early AD. For up-to-date information, see www.adni-info.org. Following a prior study (Shen et al., 2010), 733 non-Hispanic Caucasian participants were included in this study.

2.1 SNP genotyping and group information

The SNP data (Bertram et al., 2007), used in this study, were genotyped using the Human 610-Quad BeadChip (Illumina, Inc., San Diego, CA, USA). Among all SNPs, only SNPs, belonging to the top 40 AD candidate genes listed on the Alzheimer database (www.alzgene.org) as of June 10, 2010, were selected after the standard quality control (QC) and imputation steps. The QC criteria for the SNP data include (i) call rate check per subject and per SNP marker, (ii) gender check, (iii) sibling pair identification, (iv) the Hardy–Weinberg equilibrium test, (v) marker removal by the minor allele frequency and (vi) population stratification. As the second pre-processing step, the quality-controlled SNPs were imputed using the MaCH software (Li et al., 2010) to estimate the missing genotypes. After that, the Illumina annotation information based on the Genome build 36.2 was used to select a subset of SNPs, belonging to the top 40 AD candidate genes (Bertram et al., 2007).

The above procedure yieldted 1224 SNPs from 37 genes. For the remaining three genes, no SNPs were available on the genotyping chip. The genes and the number of their SNPs are shown in Figure 1.

Fig. 1. Top 37 AD risk factor genes used in this study and the numbers of their SNPs.
SNPs in our learning model so as to achieve more lucid relationships between SNPs and neuroimaging phenotypes.

Besides grouping SNPs by genes, an alternative method could be based on LD. Through estimating non-random association of alleles at different loci (e.g., using pairwise correlation coefficients $r^2$, as shown in Figure 2), the relationships between SNPs in terms of genetic linkage are established. For example, the group structure can be clearly observed in Figure 2 where a group is defined as a block of SNPs whose pairwise $r^2 \geq 0.2$. As a result, we have 185 groups comprising 1029 SNPs, with each of the remaining 195 SNPs being isolated by itself.

In this study, we consider grouping SNPs by both genes and LD correlation coefficients $r^2$.

2.2 MRI analysis and extraction of imaging genotypes

Two widely employed automated MRI analysis techniques were used to process and extract imaging genotypes across the brain from all baseline scans of ADNI participants as previously described [19]. First, voxel-based morphometry (VBM) [20] was performed to define global gray matter (GM) density maps and extract local GM density values for target regions. Second, automated parcellation via FreeSurfer V4 [21] was conducted to define volumetric and cortical thickness values for regions of interest (ROIs) and to extract total intracranial volume (ICV). Further information is available in [19]. While a complete investigation of all VBM and FreeSurfer measures is an interesting future direction, this study focuses on a subset of these measures to test the proposed methods. Ten VBM (GM density) measures and 12 FreeSurfer measures (thickness/volume), which are known to be related to AD, are selected as QTs for identifying QTLs. These QTs are extracted from roughly matching ROIs with VBM and FreeSurfer. Table 1 shows the description of these QTs and Figure 3 maps some of these ROIs in the brain space. All these measures were adjusted for the baseline age, gender, education, handedness and baseline ICV using the regression weights derived from the healthy control participants.

Table 1. QTs from 'matching' ROIs: the volumetric/thickness measures (FreeSurfer) and GM density measures (VBM)

<table>
<thead>
<tr>
<th>Volume/Thickness (ID and ROI)</th>
<th>GM Density (ID and ROI)</th>
</tr>
</thead>
<tbody>
<tr>
<td>LHippV ol</td>
<td>LHippocampus</td>
</tr>
<tr>
<td>RHippV ol</td>
<td>RHippocampus</td>
</tr>
<tr>
<td>LEntCtx</td>
<td>LParahipp</td>
</tr>
<tr>
<td>REntCtx</td>
<td>RParahipp</td>
</tr>
<tr>
<td>LPrecuneus</td>
<td>LPrecuneus</td>
</tr>
<tr>
<td>RPrecuneus</td>
<td>RPrecuneus</td>
</tr>
<tr>
<td>LMeanFront</td>
<td>LMeanFrontal</td>
</tr>
<tr>
<td>RMeanFront</td>
<td>RMeanFrontal</td>
</tr>
<tr>
<td>LMeanLatTemp</td>
<td>LMeanLatTemporal</td>
</tr>
<tr>
<td>RMeanLatTemp</td>
<td>RMeanLatTemporal</td>
</tr>
</tbody>
</table>

3 METHODS

In this section, we first systematically develop our computational models to explore the associations between SNPs and imaging phenotypes. As illustrated in Figure 4, our method mainly addresses the group structure of genetic markers and joint learning across all the imaging endophenotypes,
To avoid overfitting and increase numerical stability, the ridge regression
is used to regularize the prediction error term $||W||_2^2$.
Figure 4, the pairwise LD correlation coefficients $r^2$ between 'rs14776413',
rs1801131' and 'rs6541003' are >0.2, thus they are more homogeneous and
should be considered together when we predict the responses of the imaging
features. Motivated by sparse learning, such as Lasso, group Lasso, and
and group Lasso, we propose a novel form of regularization as follows:
$$
\min_{W} \sum_{i=1}^{n} ||Wx_i - y_i||_2^2 + \gamma \sum_{m=1}^{K} \sum_{c=1}^{N_m} ||w_{i,c}||_2,
$$
where the SNPs, i.e. features, are partitioned into $K$ groups $\Pi = \{\pi_1, \ldots, \pi_K\}$,
such that $\{w_{i,c}\} \in \pi_c$ are genetically linked, and $m_c$ is the number of SNPs in $\pi_c$.
Two types of genetic links are used here to group SNPs: (i) SNPs are naturally
divided into groups based on their belonging or nearest genes. (ii) SNPs are
grouped by thresholding the pairwise LD correlation coefficients $r^2$, e.g.
in this work, the neighboring SNPs whose $r^2 \geq 0.2$ form a group.

### 3.1 G-SMuRFS

To explore the associations between SNPs and continuous imaging
phenotypes, the linear (least square) regression (LR) is a standard approach.
To avoid overfitting and increase numerical stability, the ridge regression (RR)
is a better option. Given the SNP data of the ADNI participants
$x = (x_1, \ldots, x_n) \subseteq \mathbb{R}^n$ and the selected imaging phenotypes
$y = (y_1, \ldots, y_n) \subseteq \mathbb{R}^n$, such that $|x_i|$, $e_{\pi_c} \in e_{\pi_c}$ are genetically linked, and $m_c$ is the number of SNPs in $\pi_c$.

#### 3.1.1 Group-sparsity for genetic association

The objective of RR model in Equation 6 suffers from a number of problems when applied to estimation of the imaging genetic associations. First, the
weight matrix $W$ is not sparse, therefore all the SNPs are involved in the
prediction of imaging phenotype responses. However, among numerous
SNPs, only a small fraction of them are relevant to specific imaging QFs. Thus, it is desirable to select only relevant SNPs for more accurate prediction.
Second, similar to LR, the tasks in the RR regression model are decoupled and each of them can be learned separately. As a result, the information of
underlying interacting relationships between the brain regions are ignored, which, though, are essential to brain functionalities. Finally, the rows of $W$ are equally treated in the RR model, which implies that the underlying
structures among these SNPs are overlooked. However, it is generally
believed that many SNPs are genetically linked. In order to tackle these
difficulties, we propose a novel G-SMuRFS method to exploit the interrelated
structures within and between the genotypes and phenotypes.
such sparsity problem as a second-order cone programming (SOCP) or algorithm to solve Equation (7). Existing algorithms usually reformulate because the number of genetic markers can be very large, we need an efficient
described in Algorithm 1.

Taking the derivative with respect to \( W \) and setting the derivative to zero, we have
\[
\begin{align*}
XX^T W - XY^T + \gamma_1 D W + \gamma_2 D^T W X &= 0, \\
&= \sum_{i=1}^{K} \left| W^T X - y_i \right|^2 + \gamma_1 \sum_{i=1}^{K} \left| W \right|_F + \gamma_2 \sum_{i=1}^{K} \left| W \right|_2.
\end{align*}
\]
which can be concisely rewritten in matrix form as:
\[
\min_{W} \sum_{i=1}^{N} \left| W^T X - y_i \right|^2 + \gamma_1 \left| W \right|_F + \gamma_2 \left| W \right|_2.
\]

In Equation (7), the first term measures the regression loss. The second term couples all the regression coefficients of a group of features across all the \( c \) tasks together, which incorporates the group information on features (SNPs) due to the genetic linkage. Finally, the third term penalizes all \( c \) regression coefficient of each individual feature as whole to select features across multiple learning tasks.

We call Equation (7) as G-SMuRFS method with illustration in Figure 4.

3.2 A new efficient optimization algorithm
Because the number of genetic markers can be very large, we need an efficient algorithm to solve Equation (7). Existing algorithms usually reformulate such sparsity problem as a second-order cone programming (SOCP) or semidefinite programming (SDP) problem, which can be solved by interior point method or the bundle method. However, solving SOCP or SDP is computationally very expensive, which limits their use in practice. Here, we propose an efficient algorithm to solve our objective function in Equation (7).

Taking the derivative with respect to \( W \), and setting the derivative to zero, we have
\[
\sum_{i=1}^{K} \left( W^T X - y_i \right) X - \gamma_1 D + \gamma_2 D^T X = 0,
\]
where \( W \) can be efficiently obtained by solving the linear equation \((XX^T + \gamma_1 D + \gamma_2 D^T)W = XY^T\), and the matrix inversion that is computationally expensive is not involved.

Note that \( D \) and \( W \) in Equation (7) depend on \( W \) and thus are also unknown variables. We propose an iterative algorithm to solve this problem, which is described in Algorithm 1.

3.3 Analysis of the algorithm
Now we prove that Algorithm 1 converges to the global optimum.

Lemmata 1. For any matrices \( M \) and \( M_0 \), with the same size, we have \(|\left|M\right|_F - \left|M_0\right|_F| \leq \left|M - M_0\right|_F \leq \left|M - M_0\right|_2 \leq \left|M - M_0\right|_\infty \).

Proof. Obviously, \( |\left|M\right|_F - \left|M_0\right|_F| \leq \left|M - M_0\right|_F \). We have
\[
2\left|M\right|_F \geq \left|M\right|_F - \left|M_0\right|_F + \left|M_0\right|_F \geq 2\left|M\right|_F - \left|M - M_0\right|_F \geq \left|M - M_0\right|_F.
\]
which completes the proof.

\[\sqrt{\frac{1}{2}(W^T X - y_i)} \leq W \]

When \( |W|_F = 0 \), the \( k \)-th diagonal block of \( D \) can be regularized as \( \frac{1}{2\sqrt{|W|_F^2 + \epsilon}} \). Then the derived algorithm can be proved to minimize \( \sum_{i=1}^{N} \left| W^T X - y_i \right|^2 + \gamma_1 \sum_{i=1}^{N} \left| W \right|_F^2 + \gamma_2 \sum_{i=1}^{N} \left| W \right|_2^2 + \epsilon \). It is easy to see that this problem is reduced to problem 2 when \( \epsilon \to 0 \).

Input: \( X = [x_1, x_2, \ldots, x_n] \in \mathbb{R}^{d \times n}, Y = [y_1, y_2, \ldots, y_n] \in \mathbb{R}^{n \times 1} \)

Initialize \( W_1 \in \mathbb{R}^{d \times c}, \gamma_1 = 1; \gamma_2 = 1; \epsilon = 10^{-4} \)

while not converge do
1. Calculate the block diagonal matrix \( D_k \), where the \( k \)-th diagonal is \( \frac{1}{2\sqrt{|W|_F^2 + \epsilon}} \).
2. \( W_{k+1} = (XX^T + \gamma_1 D_k + \gamma_2 D_k^T)\gamma_1^{-1}XY^T \).
3. \( t = t + 1 \).
end
Output: \( W_t \in \mathbb{R}^{d \times c} \)

Algorithm 1: Algorithm to solve Equation (7).

Theorem 1. Algorithm 1 increases the objective value in each iteration.

Proof. In each iteration \( t \), according to Step 2 we have
\[
\left|\left|W_{k+1}^T X - y \right|^2 + \gamma_1 \sum_{i=1}^{N} \left| W_{k+1} \right|_F + \gamma_2 \sum_{i=1}^{N} \left| W_{k+1} \right|_2 \right| \\
\leq \left|\left|W_k^T X - y \right|^2 + \gamma_1 \sum_{i=1}^{N} \left| W_k \right|_F + \gamma_2 \sum_{i=1}^{N} \left| W_k \right|_2 \right| + \epsilon
\]
\[
\leq \left|\left|W_k^T X - y \right|^2 + \gamma_1 \sum_{i=1}^{N} \left| W_k \right|_F + \gamma_2 \sum_{i=1}^{N} \left| W_k \right|_2 \right| + \epsilon.
\]
Applying Lemma 1 to Equation (8), we have the following
\[
\left|\left|W_{k+1}^T X - y \right|^2 + \gamma_1 \sum_{i=1}^{N} \left| W_{k+1} \right|_F + \gamma_2 \sum_{i=1}^{N} \left| W_{k+1} \right|_2 \right| \\
\leq \left|\left|W_k^T X - y \right|^2 + \gamma_1 \sum_{i=1}^{N} \left| W_k \right|_F + \gamma_2 \sum_{i=1}^{N} \left| W_k \right|_2 \right| + \epsilon
\]
Thus, Algorithm 1 increases the objective value in each iteration.

Algorithm 1 stops when the following criterion is satisfied:
\[
||W_{k+1}^T X - Y||_F / \max(||W_k^T X, 1||) \leq TOL,
\]
where \( TOL = 10^{-4} \) is empirically selected in our experiments.

Upon convergence, \( W_t, D_t, and D_t \) will satisfy Eq. 7. As the problem of solving Eq. 7 is a convex problem, satisfying the Eq. 7 indicates that \( W_t \) is a global optimum solution to Eq. 7. Therefore, Algorithm 1 converges to the global optimum of Eq. 7. Since we have a closed form solution in each iteration, our algorithm converges very fast, which makes our method suitable for not only candidate SNP, but also GWASs.

4 EXPERIMENTAL RESULTS AND DISCUSSIONS
In this section, we evaluate the proposed G-SMuRFS method by applying it to the data from the ADNI cohort, where a wide range of SNPs are examined and selected to predict the response of the MRI imaging phenotypes. The goal is to select a compact set of SNPs while maintaining high predictive power.

4.1 Improved imaging phenotype prediction
We first evaluate the proposed method in predicting the continuous responses of candidate neuroimaging phenotypes. Given two sets of imaging phenotypes, FreeSurfer and VBM, we conduct experiments on each of them separately.

We compare our method against multivariate linear regression, RR and multi-task feature learning (MTFL) [Argyriou et al. 2005].
the parameters in the range of the average results. For each of the five trials, within the training test case, we conduct standard 5-fold cross-validation and report phenotypes; (formal comparison, while the cross-validation trials in each experiment perform very
http://ranger.uta.edu/~heng/imaging-genetics/.

In cross-validation are available in the Supplementary Material at

of a single SNP over all the tasks as the SNP weight, from which MTFL method and our method. For each trial, from the learned

whereas those of the other methods are sensitive to experimental

interesting imaging QTs. In sum, the above evidence demonstrates

Clearly, the proposed approach is able to identify the most important

mixing them together may perturb the prediction. Grouping by LD blocks using r^2 yields more homogeneous groups and has a potential to boost the prediction power.

Figure 5 shows heat maps of prediction errors on each QT. While these QTs are AD-relevant, Figure 5 also shows that they are affected in different degrees by genetic factors. QTs that are better predicted by SNPs include GM density measures of the parahippocampal gyrus and frontal region in VBM analyses and thickness measures of the frontal region, lateral temporal region and precuneus in FreeSurfer analyses. The VBM and FreeSurfer measures of a certain region yield similar results in some cases (e.g. frontal region), but may provide different information in other cases (e.g. parahippocampal gyrus). Thus, performing both VBM and FreeSurfer analyses can help identify useful imaging phenotypes and guide further investigation to better elucidate the underlying disease mechanism, from gene, to brain structure and function, and to symptoms.

4.2 Genetic marker selection

Shown in Figure 4 are the regression coefficients for top 10 selected SNPs. First, these SNPs are either AlzGene candidates or proximal to the candidates; however, little is known about their underlying mechanisms in relation to AD. The results shown in Figure 4 can help identify relevant QTs for each SNP and has a potential to gain biological insights from gene to brain to symptoms. Second, as expected, the APOE SNP rs429358 shows the strongest association with all QTs in each experiment; and the hippocampal measures exhibit the strongest association with the APOE SNP. Clearly, the proposed approach is able to identify the most important AD genetic risk factor via imaging QTs as well as the best-known neurodegenerative marker. Third, besides confirming the prior findings, our method also yielded new discoveries such as the associations between APOE and other eminent AD markers including entorhinal cortex and parahippocampal gyrus. These associations were not identified in our prior massive univariate analyses on the same data (Shen et al., 2010), indicating that the proposed multilocus method has increased power to discover interesting imaging QTs. In sum, the above evidence demonstrates not only the effectiveness of the proposed method, but also the strength of using imaging QTs in genetic association study.

Quite a few SNPs from the SORCS1 gene are selected as the top 10 hits in each experiment; however, the large size of the gene (Fig. 4) may play a role. Figure 5 shows an LD plot with location maps for a group of 46 SNPs, where two top hits (red spikes) are highlighted for each of the FreeSurfer and VBM experiments. Although SORCS1 has been associated with

Table 2. The results (P-values) of t-tests for performance comparison between our methods and three competing methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Group by gene</th>
<th>Group by r^2 &gt; 0.2</th>
<th>Group by r^2 &gt; 0.5</th>
<th>Group by gene</th>
<th>Group by r^2 &gt; 0.5</th>
</tr>
</thead>
<tbody>
<tr>
<td>MLR</td>
<td>7.08 × 10^{-4}</td>
<td>3.13 × 10^{-4}</td>
<td>9.28 × 10^{-6}</td>
<td>3.96 × 10^{-6}</td>
<td></td>
</tr>
<tr>
<td>RR</td>
<td>1.31 × 10^{-2}</td>
<td>2.21 × 10^{-3}</td>
<td>2.12 × 10^{-2}</td>
<td>1.85 × 10^{-3}</td>
<td></td>
</tr>
<tr>
<td>MTFL</td>
<td>6.57 × 10^{-3}</td>
<td>2.41 × 10^{-7}</td>
<td>5.82 × 10^{-7}</td>
<td>2.63 × 10^{-7}</td>
<td></td>
</tr>
</tbody>
</table>

Fig. 5. Performance comparison: The mean and SD of the root mean square errors (RMSEs) obtained from five cross-validation trials in each experiment are plotted, where each error bar indicates ±1 SD. (a) FreeSurfer imaging phenotypes, (b) VBM imaging phenotypes.
Identifying quantitative trait loci via group-sparse multi-task regression and feature selection

Fig. 6. (a and b) Show the heat maps of RMSEs for predicting VBM (a) and FreeSurfer (b) measures using LR, RR, our G-SMuRFS method with SNPs grouped by gene and G-SMuRFS with SNPs grouped by $r^2 > 0.2$, where top 10 SNPs were used in our G-SMuRFS methods. In (c), RMSEs for predicting VBM measures using four methods are mapped onto the brain volume.

Fig. 7. Regression coefficients are visualized for top 10 selected SNPs in each of the four experiments (from top to bottom): (i) group by $r^2 > 0.2$, regression on VBM measures; (ii) group by gene, regression on VBM measures; (iii) group by $r^2 > 0.2$, regression on FreeSurfer measures; and (iv) group by gene, regression on FreeSurfer measures.

diabetes and AD (Lane et al., 2010), the top ranked SORCS1 SNPs in Figure 7 have not been reported in prior association studies. Thus, this gene together with its SNPs warrants further investigation in independent cohorts. Due to the nature of our method, an epistasis analysis on these top hits would be appropriate for investigation in future studies.

Fig. 8. Pair-wise LD in a group of 46 SNPs proximal to SORCS1. Numerical values $r^2$ of the LD maps are determined by Haploview and visualized with WGAViewer. The top panel is the ideogram of the chromosome and the vertical red line represents the relative location of the locus of interest. In the second panel, regression coefficients*100 is plotted for each SNP for the FreeSurfer data, where two top hits rs765651 and rs1931600 are labeled with red lines. In the third panel, regression coefficients*100 is plotted for each SNP for the VBM data, where two top hits rs1931600 and rs1936488 are labeled with red lines. The fourth panel shows the recent selection score (Voght et al., 2006). The bottom figure demonstrates the LD pattern among 46 SNPs.
5 CONCLUSIONS

In this article, we have proposed a novel G-SmORFS method to perform both regression analysis for predicting continuous responses of brain imaging measures and selecting relevant SNPs in an MCI/AD study. Different from traditional regression methods that ignore the interrelated structures within genotyping and imaging data, our method studies the associations between SNPs and imaging phenotypes within a single regression framework and shared common subspace. Through enforcing a new form of regularization using $G_{2,1}$-norm that takes into account both group-level structural information inside SNP data and sparsity among SNP groups, our proposed model is able to exploit additional information to achieve both enhanced predictive performance and improved feature (SNP) selection capability. Besides, $G_{2,1}$-norm regularization is used in our model to jointly select SNPs relevant to important imaging phenotypes. An efficient algorithm to solve the proposed objective is presented with rigorous proof of its correctness and convergence. Our experiments using the SNP and MRI data from the ADNI cohort yielded the following promising results: (i) the prediction performance of G-SmORFS method was consistently better than conventional multi-variate linear regression and ridge regression; (ii) a compact set of SNP predictors were identified in each test case, warranting further investigation in independent cohorts for confirmation; and (iii) these selected SNPs could predict the responses of multiple imaging phenotypes at the same time and had a potential to serve as useful genetic risk factors for AD. These promising results were consistent with our theoretical foundation and in accordance with some prior studies, which demonstrated the effectiveness of the proposed method.

One important future direction of this work could be to explore the possibility of simultaneously employing multiple SNP grouping schemes or more generally adopting a pre-defined network/pathway strategy and see whether these approaches can further improve the prediction performance. Other potential future directions include (i) application of G-SmORFS method to additional imaging phenotypes (e.g., PET, MRI data); and (ii) building a principled sparse learning framework to reveal complex relationships among phenotypes (e.g., PET, fMRI data); and (ii) building a principled prediction performance. Other potential future directions include (i) application of G-SmORFS method to additional imaging phenotypes (e.g., PET, MRI data); and (ii) building a principled sparse learning framework to reveal complex relationships among phenotypes (e.g., PET, fMRI data); and (ii) building a principled prediction performance.

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REFERENCES


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