

# The Pinhole Camera

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## Imaging without Lenses or Mirrors

By Matt Young

I like to imagine that the pinhole camera was the third imaging system invented. First was the window, which is perhaps half-a-million years old and was invented for looking through walls. (This is the origin of the old joke, "Did you hear of the person who invented a device for looking through walls?" "No, what is it called?") The plane mirror was, I assume, invented just after the beginning of the bronze age, about 6000 years ago. A little reflection will show that its function was for looking at yourself. If modern practice is anything to go by, the inventor was a teenager.

The Greeks apparently understood the principle of the pinhole camera and developed convex mirrors and burning glasses as well. The Greeks, however, are not remembered for their ability to putter around, so the pinhole camera waited in the wings for almost 1500 years. Alhazen (Ibn Al-Haytham), whom D.J. Lovell<sup>1</sup> called the greatest authority on optics in the Middle Ages, lived around +1000 on the Gregorian calendar, invented the pinhole camera, and explained why the image was upside down. He also studied the optics of the eye and used the Arabic word for lentil to describe the lens of the eye. Indirectly, therefore, he gave us the modern English word, lens, which is the Latin word for lentil.

Leonardo da Vinci may have used the pinhole camera in the 1500s for his studies of perspective.<sup>2</sup> Around 1600, Della Porta reinvented the pinhole camera.<sup>3</sup> Apparently

he was the first European to publish any information on the pinhole camera and is sometimes incorrectly credited with its invention. Della Porta's pinhole camera was a large, dark room with a fairly sizeable hole in one wall. He may have coined the term camera obscura, which is Latin for dark room. Our English word camera, therefore, derives from the Latin word for room or chamber. Della Porta also enlarged the hole and used lenses to cast a sharper, brighter image, though he was probably not the first to use lenses in this way.

Despite its antiquity and apparent simplicity, the pinhole camera offers several advantages over lens optics, particularly when resolution is not especially important. These include

- complete freedom from linear distortion
- depth of field from a few centimeters to infinity
- wide angular field

The pinhole's light-gathering ability is poor, but this is largely offset by the high sensitivity of modern films and television cameras. In addition, pinholes can be used in the ultraviolet and x-ray regions of the spectrum when reflecting or refracting materials are not readily available.

Within the last 20 years or so, the pinhole camera has been used to image x-rays, to provide great depth of field in a flight simulator, to produce multiple images for integrated circuit masks, for fine art photography, and to help certain scientists keep their families well fed. In addition,



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a few years ago a small company marketed a pinhole camera that used real photographic film. The camera was called the PinZip, on the notion that the photons go "Zip" as they pass through the pinhole and hit the film.

There is now a *Pinhole Journal*<sup>4</sup> and also a book on pinhole "fotografy."<sup>5</sup> I take it that you are supposed to pronounce fotografy differently from photography, but I haven't quite mastered the sounds yet.

### Practical Pinhole Cameras

The classic pinhole camera is made by taping a sheet of  $4 \times 5$ - or  $8 \times 10$ -in film to the inside of a certain kind of cylindrical oatmeal box whose manufacturer's name the National Institute of Standards and Technology's policy forbids me to print. In any case, the film is taped to the cylindrical part of the box, not the ends, and a hole is punched into the cylinder opposite the film. The box is taped shut, and the camera is ready. Purists will use no other kind of pinhole camera, even though the curved film plane causes distortion.

You can also make a pinhole camera out of a single-lens reflex camera body and a cardboard tube or, if you want to get fancy, a set of extension tubes. You'll have to cover your head with a black cloth or use an old-fashioned camera with a sports finder, because it is hard to see anything on the viewing screen. A 100-mm focal length is convenient and corresponds to a "telephoto" lens in normal photography. The corresponding pinhole diameter is about 0.5 mm and is very easily punched into 50- $\mu\text{m}$  (0.002-in) brass shim stock. Place the shim stock on top of a sheet of corrugated cardboard. Take a sharp, 0.5-mm sewing needle and tap it gently with a small tool until it pierces the brass. Grasp the needle between your thumb and forefinger, rotate it, and force it through the brass. (With practice, you can manufacture holes under about 0.2 mm. See Reference 6 for information about an array of precisely sized, 25- $\mu\text{m}$  pinholes.) Rub both sides of the brass gently with very fine emery cloth and clean with soap and water.

To attach the pinhole to your camera, you will need lots of black electrical tape or black masking tape; hence, Mrs. Young's Law: Science as we know it would not exist if it weren't for masking tape.

If you use about a 100-mm focal length and a 0.5-mm pinhole, the F-number will be about 200. The F-number of a lens is the ratio of its focal length to its diameter and is a measure of the lens's light-gathering ability. If this ratio is equal to 16, for example, we write F/16, which is pronounced "eff sixteen." Typical lenses have variable apertures that are calibrated with discrete F-numbers (called F-stops) of 4, 5.6, 8, 11,.... This is an ascending sequence with the common ratio of  $\sqrt{2}$ . As the F-numbers in the sequence increase, the lens's light-gathering ability, which is proportional to the area of the aperture, decreases by factors of 2. Exposure times, or shutter speeds, are similarly calibrated in factors of 2; typical exposure times,

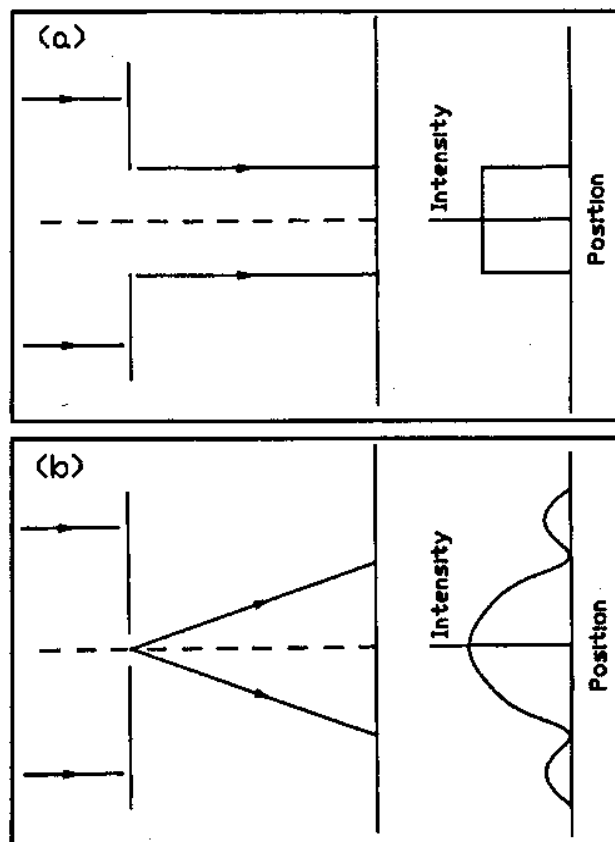


Fig. 1. Pinhole camera imaging a distant point. (a) Large pinhole, geometrical optics. (b) Small pinhole, farfield diffraction.

in seconds, are 1/250, 1/125, 1/60, 1/30,.... Every time you increase the F-number by a factor of  $\sqrt{2}$ , you must increase the exposure time by a factor of 2. A typical exposure in outdoor photography is F/11 and 1/100 s.

Photographers use a rule of thumb that you can hand-hold a camera provided that the exposure time is shorter than or equal to the reciprocal of the lens's focal length; for our 100-mm pinhole camera, this means about 1/100 s. Conventional lenses, however, have resolving powers about equal to 50 lines/mm; the corresponding figure for the pinhole camera is a few lines per millimeter. You can therefore tolerate perhaps 20 times more blur due to the shaking of your hand, so let us say that you can hand-hold your pinhole camera to about 1/5 s.

Another rule of thumb states that the exposure in bright sunlight is about F/16, with an exposure time equal to the reciprocal of the film's ISO speed. (The ISO speed is a measure of the film's sensitivity; the higher the ISO speed, the higher the sensitivity.) For example, if the ISO speed is 400, the correct exposure is about F/16 and 1/400 s. This is about equivalent to F/200 and 1/5 s. Therefore, with a fast film, you can take pictures in sunlight with your pinhole camera if you have a steady hand. Otherwise, you will need a tripod.

Theory of the Pinhole Camera

The imaging device of the pinhole camera is a hole punched through an opaque material. The image of a distant point is simply the shadow of the hole—or rather the shadow of the material around the hole. That is, the image is a bright spot on a dark background. When the hole is large, the image of the distant point is large and displays a diameter equal to that of the pinhole [Fig. 1(a)].<sup>7</sup>

An extended object is a collection of points; its image is therefore a collection of spots. The smaller the spots, the finer the detail that can be discerned in the object. Therefore, in many ways, the best pinhole is the one that produces the smallest image of a point.

If we make the pinhole very small in an effort to improve resolution, we will arrive at the situation depicted in Fig. 1(b). Here, the hole is so small that the pattern of light in the film plane is an Airy disk: the Fraunhofer, or farfield, diffraction pattern of the pinhole.<sup>8</sup> In this region, the smaller the hole, the larger the spot. Evidently, the pinhole that gives the smallest spot lies in the region between the geometrical optics region depicted in Fig. 1(a) and the region of farfield diffraction depicted in Fig. 1(b).

Figure 2, a graph of image radius as a function of pinhole radius, expresses this consideration. When the pinhole is very small, the image radius  $r$  is the radius of the Airy disk, or  $0.61\lambda f/s$ , where  $s$  is the radius of the pinhole and  $\lambda$  is the wavelength of the light. (If we express the radius of the Airy disk in terms of the diameter  $D$  of the pinhole, we get the more common expression  $1.22 \lambda/D$ .) This equality is represented by the hyperbola in Fig. 2. On the other hand, when the pinhole is large, the image radius  $r$  is equal to the pinhole radius  $s$ , as represented by the line in Fig. 2.

The curve intersects the line where  $0.61\lambda f/s = s$ , or, roughly, where

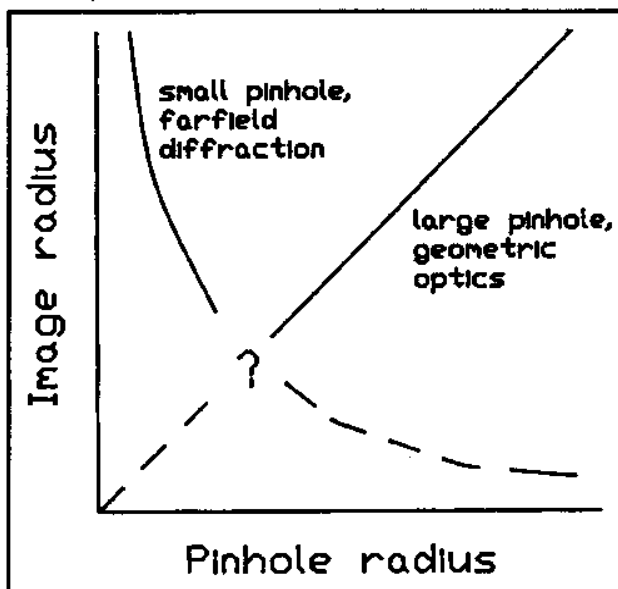


Fig. 2. Image radius as a function of pinhole radius.

$$f = \frac{s^2}{\lambda} \tag{1}$$

Neither the hyperbola nor the line accurately represents reality in this region, yet this is the region we are most interested in because the pinhole camera gives the sharpest images there. This is the region between nearfield and farfield diffraction; here, the image is not amenable to description by simple arguments.

Two-Point Resolution

Usually, we are more interested in distinguishing between neighboring points or lines than in isolated points. Hence, we change our focus from image radius to resolution limit—the smallest discernible separation between two image points. In the farfield case [Fig. 3(a)], when the image of a single point is an Airy disk, the resolution limit is the radius  $0.61\lambda f/s$  of the Airy disk. In the geometrical optics case [Fig. 3(b)], we use a good deal of hindsight and assume that the resolution limit is 1.5 times the radius  $s$  of the image—that is, of the pinhole itself.

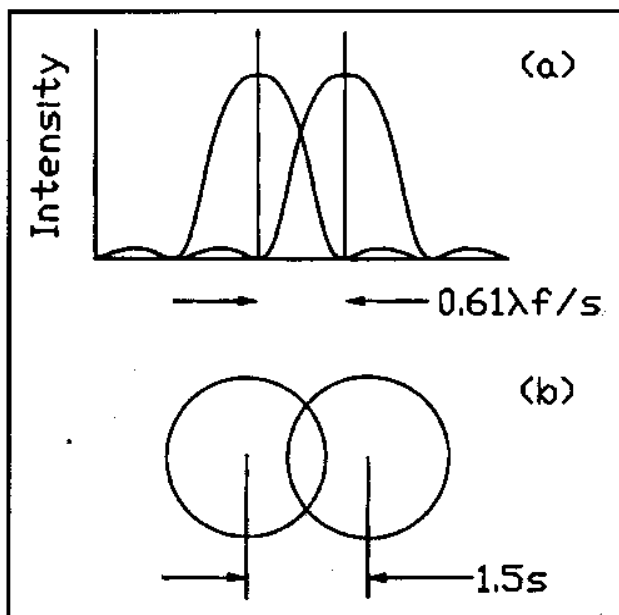


Fig. 3. Limit of resolution. (a) Farfield diffraction, Rayleigh criterion. (b) Geometrical optics, uniform disks.

In physics you can make your reputation by judicious use of the first two terms in a Taylor series or by your ability to define normalized expressions. There seems to be no opportunity to use a Taylor series here, so let us try normalization. We define normalized resolution limit as resolution limit divided by pinhole radius and normalized focal length as focal length divided by  $s^2/\lambda$ . This allows us to perform experiments with a number of pinholes or focal lengths and to compare the results. In addition, it allows us to redraw Fig. 2 as two intersecting lines (Fig. 4) instead of an intersecting line and a curve. Because of the use of

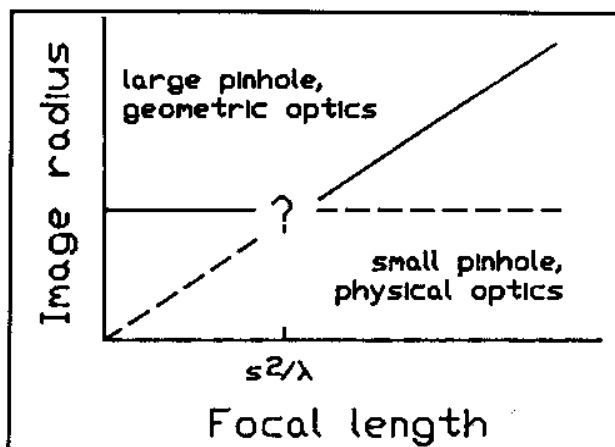


Fig. 4. Figure 2 redrawn in terms of normalized focal length.

normalized variables, we can now plot data for any pinhole size or focal length on a single graph.

### Experiment

I performed a resolution experiment using as a light source a 650-W, quartz-iodine lamp intended for home

movies. To reduce stray light, the lamp had to be enclosed in a metal housing and then cooled with forced air. In addition, since the beam could easily set cardboard on fire at a distance of 50 or 60 cm, I passed the light through about 10 cm of distilled water and a heat-absorbing filter. By the time the water began to boil, I usually needed a break anyway; the heat-absorbing filter would have cracked without the water as a prefilter. The lamp and the filters illuminated a resolution target that was in contact with both a ground glass and a gelatin filter that provided more-or-less monochromatic light at 500 nm.

The target was a three-bar target that had both horizontal and vertical bars. Figure 5 shows photographs taken with different conditions. The largest bars in the target have spatial frequency of 1 line/mm.

The photographs in the left column were taken on the axis of the system; those in the right column were taken 45° off axis. Similarly, the photographs in the top row were taken with the focal length of the camera equal to  $s^2/\lambda$ ; those in the bottom row were taken with the focal length equal to about four-tenths of that value.

The sharpest photograph is Fig. 5(a). Figure 5(b) shows astigmatism: along the right edge, the fifth and sixth horizontal bars are not resolved, whereas the corresponding vertical bars are resolved. This is so because the pinhole appears oval when viewed off axis. Both photographs taken with the shorter focal length also display spurious resolution. Several of the sets of three bars are unresolved but appear as two bars, 180° out of phase with the original three bars. As a result of astigmatism, the left-most bars of Fig. 5(d) show both true resolution and spurious resolution at the same spatial frequency. Figure 6 is easily worth a thousand words, since it explains spurious resolution with no need for elaboration.

Figure 7 is a plot of normalized resolution limit as a function of the focal length of the camera expressed in units of  $s^2/\lambda$ . The solid lines are the predicted values, as in Fig. 4. The data were actually taken with three different pinholes under different conditions.<sup>6</sup> Agreement with the simple theory is quite good over most of the range. The resolution limit is smallest when the focal length of the camera is about equal to  $s^2/\lambda$ , and there is a (weak) focus at this distance from the pinhole. (The scale change where  $f = s^2/\lambda$  somewhat exaggerates the sharpness of the focus.) We could call  $s^2/\lambda$  the natural focal length of the pinhole, and, indeed, the pinhole

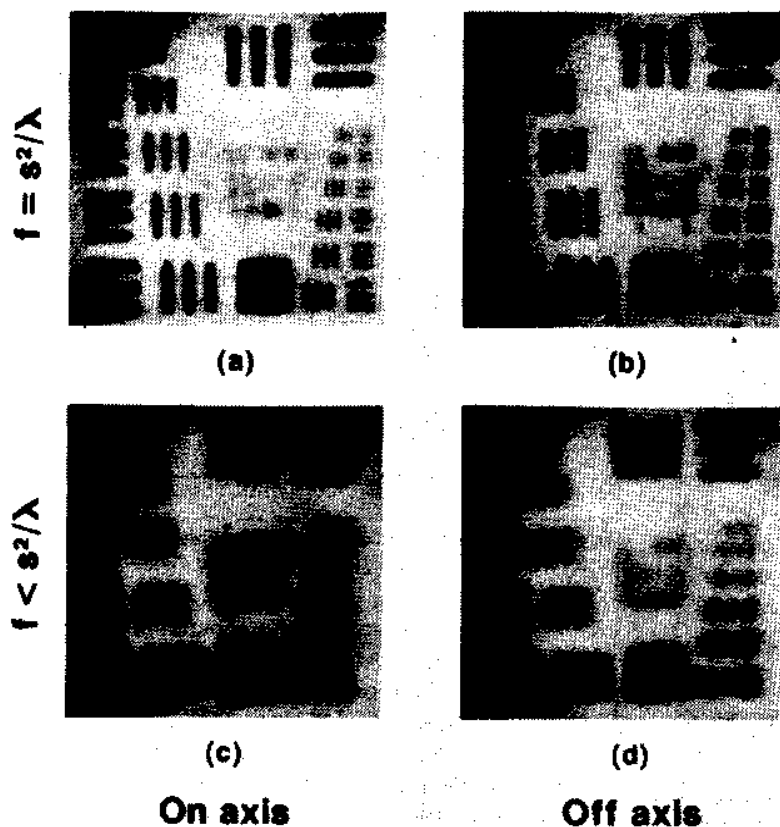


Fig. 5. Resolution target photographed with a pinhole camera. The largest bars have a spatial frequency of 1 line/mm. The upper targets were photographed with the optimum pinhole diameter, the lower with a pinhole several times larger. Note spurious resolution in (c) and (d) and astigmatism in (b) and (d).

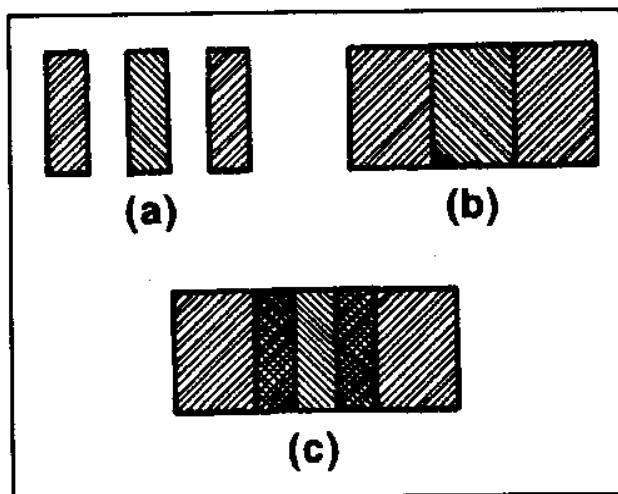


Fig. 6. The cause of spurious resolution. Three bars (a) well resolved, (b) unresolvable, and (c) displaying spurious resolution.

behaves much like a lens with this focal length. For example, if you wanted to take a picture of a nearby object, you would apply the lens equation with  $f = s^2/\lambda$ . If the object and image distances were not those given by the lens equation, the pinhole camera would be out of focus and resolution would suffer. If anything, the pinhole should be a little bit large, to increase its light-gathering ability. If, however, the pinhole is about 20 percent larger than optimum, the light-gathering power will increase by only 40 percent, whereas resolution will worsen by roughly a factor of 2.

Figure 7 also has a hatched area that indicates spurious resolution. Spurious resolution is found only when the pinhole camera is defocused so that the image distance is too short for the pinhole or, equivalently, so that the pinhole is too large for the image distance. We also find spurious resolution with defocused lenses and, sometimes, in the images of lenses that have aberrations.

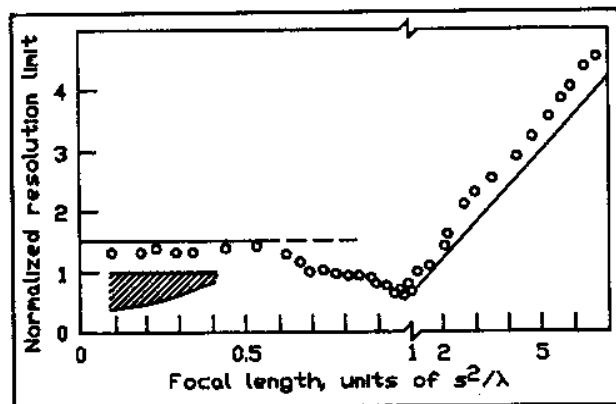


Fig. 7. Experimental data: Resolution limit in units of the pinhole radius as a function of focal length in units of the natural focal length  $s^2/\lambda$  of the pinhole. Resolution limit is least when  $f = s^2/\lambda$  and the pinhole occupies a single Fresnel zone. The hatched region indicates spurious resolution, which occurs only when the normalized focal length is less than about 0.4.

### Nearfield and Farfield

Figure 7 can be regarded as a sketch of the way in which light propagates through an aperture. It is redrawn and annotated as Fig. 8. Close to the aperture, the illuminated area is just the geometrical shadow of the aperture itself. Farther from the aperture, diffraction effects begin to become apparent. This is the region of nearfield diffraction, sometimes called the Fresnel diffraction region. In this region, the diffraction pattern is not predictable from simple arguments but consists of concentric bright and dark rings. The intensity on the axis might be a maximum, a minimum, or an intermediate value. As we approach the distance  $s^2/\lambda$ , the number of rings decreases, and, finally, the diffraction pattern becomes one main lobe surrounded by weak rings. Only at the distance  $s^2/\lambda$  and beyond does the beam acquire the divergence  $0.61\lambda/s$  (or  $1.22\lambda/D$ ) usually associated with farfield, or Fraunhofer, diffraction. Mathematically, the pattern does not approach the Airy disk until several times this distance.

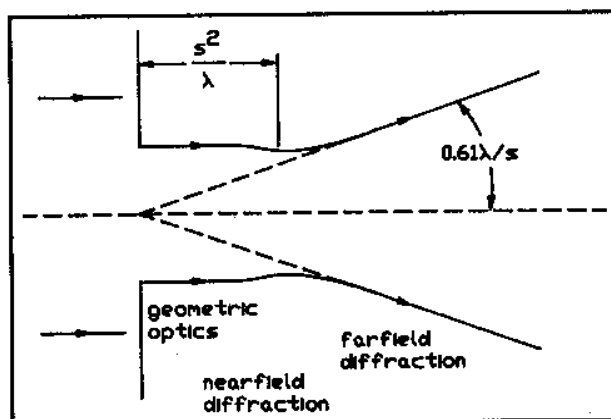


Fig. 8. Figure 7 redrawn to show the envelope of the beam that passes through an opening. Near the opening, we see the geometrical shadow; farther away, we see Fresnel or nearfield diffraction patterns and, finally, Fraunhofer or farfield patterns. The beam does not acquire the farfield beam divergence  $0.61\lambda/s$  until it has propagated a distance greater than  $s^2/\lambda$  beyond the opening.

The common remark that you can observe diffraction only when the aperture diameter approaches the wavelength is therefore not true. You can observe nearfield diffraction no matter how large the aperture is. Provided that the edge of the aperture is not rough, the pattern very close to the aperture closely approximates an edge diffraction pattern. Likewise, you can always observe a farfield pattern if you can get far enough away. For example, if the diameter of the aperture is about 1 mm, or  $2000\lambda$ , the farfield region begins only 0.5 m from the aperture. Similarly, you can find the farfield distance of an arbitrary or irregular aperture by squaring a typical dimension and dividing by the wavelength.

### Optimum Focal Length

The natural focal length of the pinhole is  $f = s^2/\lambda$ ; with visible light, whose wavelength is about 550 nm, this translates to a pinhole diameter

$$D = 0.047 \sqrt{f} \quad (2)$$

when  $D$  and  $f$  are expressed in millimeters. Since the optimum pinhole diameter increases as the square root of the focal length, you can improve the detail in the image by scaling everything up. For example, if you quadruple both the focal length and the size of the film, you will retain the same field of view while only doubling the pinhole diameter. Resolution is thereby improved by a factor of 2, since the ratio of the film size to the resolution limit has been doubled. In the jargon of modern optics, we would say that there are more pixels (picture elements) in the larger format. In rough numbers, a 35-mm format with 50-mm focal length is about 180 pixels wide, whereas a 100 × 127-mm (4 × 5-in) format with 150-mm focal length is about 340 pixels wide, or about the same as a TV image. Since the picture is two-dimensional, the larger format carries about four times the information. Nothing is free, however; the larger format also has a higher F-number, or lower light-gathering ability, so the exposure time is longer.

### Off-Axis Imagery

The ability to expose very wide-angle photographs is limited by loss of exposure in the corners of the image. The problem is not unique to the pinhole camera but afflicts nearly all optical systems. Suppose that a small area is imaged off the axis of the pinhole camera by angle  $\theta$  (Fig. 9). From the image plane the pinhole appears as a bright spot of light. The off-axis image is farther from the pinhole by  $1/\cos \theta$  so, according to the inverse-square law, the irradiance there is less by  $\cos^2 \theta$ . In addition, the pinhole appears smaller by  $\cos \theta$  because of the obliquity. Finally, the light falls obliquely onto the film plane and therefore covers an area  $1/\cos \theta$  larger than the equivalent area on the axis.

These three effects combine to reduce the exposure at the off-axis point by a factor of  $\cos^4 \theta$ . This is the famous and infamous cosine-fourth law. If, for example, we wish

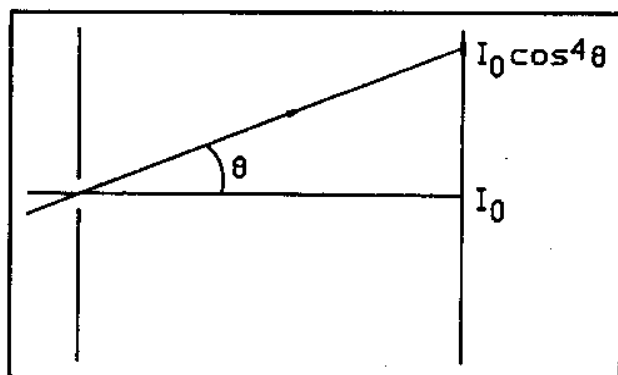


Fig. 9. Cosine-fourth law. The exposure off the axis by an angle  $\theta$  is reduced by the factor  $\cos^4 \theta$ .

to cover a 60° field of view (30° half-angle), then  $\cos^4 30^\circ = 0.56$ , and we suffer a loss equivalent to one F-stop of exposure between the center and the edge of the image. For a 90° field,  $\cos^4 45^\circ = 1/4$  or two F-stops. Most of the time, this is far too much loss of exposure to be acceptable.

You can get around the cosine-fourth law by using a cylindrical film "plane" centered around the pinhole. Then, the cosine-fourth law reduces to a simple cosine law. Since  $\cos 45^\circ = 0.71$ , you can cover a 90° field with a loss of exposure of only one-half of an F-stop. That is one reason those purists like their oatmeal boxes.

### Franke's Widefield Camera

In 1979, Franke invented the widefield pinhole camera shown in Fig. 10.<sup>9</sup> If its index of refraction is about 1.5, the glass or plastic hemisphere reduces a 90° field of view to 42°. Even a moderate purist like me will agree that this is a pinhole camera. The actual imaging device is the pinhole, and the hemisphere is just a field lens, or a lens that increases the field of view but does not itself project an image.

Franke found that there is slight distortion beyond about 70° because  $\sin \theta \neq \theta$ , and that the best index of refraction would be 1.3. This is the index of refraction of water, and, in fact, R.W. Wood once submerged a pinhole camera in water to achieve the same effect.

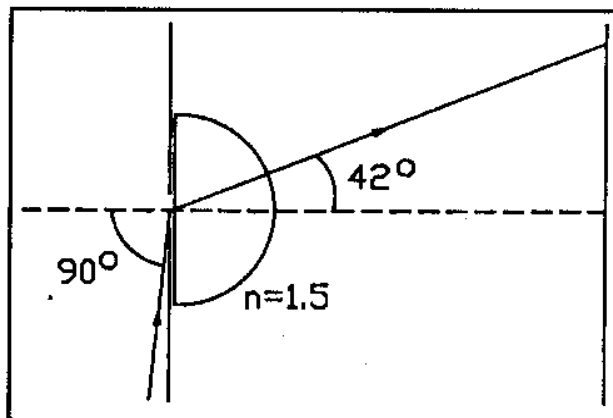


Fig. 10. Franke's widefield pinhole camera. If the index of refraction of the hemispherical field lens is about 1.5, the hemisphere is compressed to a 42° cone.

### Fresnel Zone Plate

The Fresnel zone plate is a relative of the pinhole camera in that it does not use mirrors or lenses for its imaging properties. Since the zone plate is covered in most optics books, I will not dwell on it, except to note that the zone plate is a sort of generalization or expansion of the pinhole camera in the plane of the aperture. The zone plate consists of a series of concentric rings, alternately clear and opaque. It works by blocking diffracted rays that would have caused destructive interference at the image point.<sup>10</sup> If the radius of the central ring of the zone plate

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is  $s$ , the focal length of the zone plate is  $s^2/\lambda$ . The pinhole camera may therefore be regarded as a zone plate with only one clear zone. Like the zone plate, it focuses by diffraction.

The zone plate, like the pinhole camera, exhibits no linear distortion. They are the only instruments I know of, except for the plane mirror, that have this property. In addition, the zone plate can be useful in the ultraviolet and x-ray regions of the spectrum, for which other imaging devices are hard to find. Self-supporting gold zone plates have been manufactured for these spectral regions.

Zone plates have resolution limits comparable to lenses with the same F-number, and they may be overlapped to form multiple images spaced by less than the diameter of the zone plates themselves. Unfortunately, the zone plate has low efficiency and suffers from veiling glare because most of the light incident on the zone plate passes through it undiffracted and falls onto the image plane.

### Cascaded Apertures

In the late 1960s, researchers at Laval University in Quebec City generalized the pinhole camera along the axis. They found that they could place several circular apertures sequentially along the axis and obtain a focus.<sup>11</sup> The positions and diameters of the apertures have to be chosen so that each aperture alone would display a near-field diffraction maximum at the desired image point. That is, each aperture must contain an odd number of Fresnel zones as seen from the image point. If there are  $N$  apertures, the intensity at that point will be increased by approximately  $N^2$ . Since energy has to be conserved, this is equivalent to sharpening the focus.

The experimental work was carried out in the microwave region and was an attempt to develop low-loss waveguides for communications. The purpose of the apertures was to keep the electric field away from the lossy walls of a conventional metallic waveguide. I have not heard of cascaded apertures since the early seventies and assume that the idea was rendered obsolete by the development of low-loss optical fiber waveguides.

### Pinspeck Camera

In the early 1980s, Adam Cohen conceived the idea of the pinspeck camera.<sup>12</sup> (I suggested that he call his paper "The Joy of Specks," but he did not take this advice.) At any rate, the imaging device is an opaque spot in the center of a larger aperture. The spot has to be large enough to cast a shadow, and the distance from the spot to the screen has to be well under  $s^2/\lambda$ . Figure 11 shows how the pinspeck camera works. Each bright object point casts a shadow of the pinspeck onto the viewing screen. If there are  $m$  resolvable object points, the intensity in each of the shadows is a fraction  $(m - 1)/m$  of what it is everywhere else. The pinspeck camera casts a very low-contrast, negative image with several times poorer resolution than a pinhole camera. Do not, incidentally, confuse the

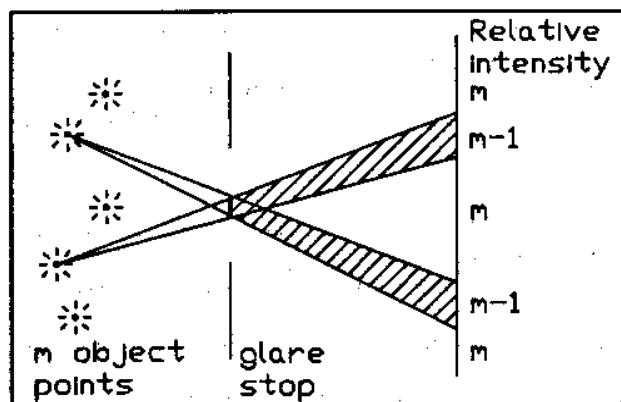


Fig. 11. Pinspeck camera. The opaque disk in the center of the glare stop casts a shadow of each bright point in the object. This results in a weak, negative image.

pinspeck camera with the Fresnel (or Poisson or Arago) bright spot.<sup>13</sup> The latter is a diffraction effect, whereas the pinspeck camera is based on geometrical optics. Diffraction will only reduce the contrast of the image.

Cohen's work was written up in *Scientific American*, along with my work and Kenneth Connors's work on the pinhole camera.<sup>14</sup> As a result of this article, we learned that the pinspeck camera had been invented just a few years before, when a group working with x-ray tubes serendipitously discovered the pinspeck principle because of metal particles lodged inside their film packs.<sup>15</sup> They now use the pinspeck camera for imaging the anode of their x-ray tubes so that they can focus the electron beam onto the anode. Because the pinspeck camera has better light-gathering capacity than the pinhole camera, the group does not risk shortening the lifetime of the x-ray tubes just to focus the electron beam. In a similar way, A.T. Young discovered the principle of the pinspeck camera due to specks of dust in a conventional camera and used the images to analyze the performance of the camera.<sup>16</sup> The contrast of the pinspeck camera is so low that photon noise affects the image and limits the camera to very simple objects.<sup>17</sup>

### Pinhead Mirror

In 1986, Thomy Nilsson, a vision scientist at the University of Prince Edward Island, accidentally discovered an image of the sun reflected off a glint in a stucco wall.<sup>18</sup> He correctly interpreted what he had seen and concluded that a tiny mirror could be used as an image-forming device, behaving just like a tiny hole. He called the mirror a pinhead mirror and asked whether it was an undiscovered imaging device.

Even those who remember history are condemned to repeat it. Three letters in *Lasers and Optronics* suggested that the pinhead mirror, like the pinspeck camera, had been invented before. For example, Donald O'Shea reported using a pinhead mirror to demonstrate a solar

eclipse to a larger number of people than would have been possible with a pinhole camera.<sup>15</sup>

Koheleth said, "Ayn kol chadash tachat ha-Shemesh" ("There is nothing new under the sun"). Who am I to argue? ♦

#### References

1. D.J. Lovell, *Optical Anecdotes*, Society of Photo-Optical Instrumentation Engineers, Bellingham, WA, 1981.
2. Ernst Mach, *The Principles of Physical Optics* (Dover, New York, n.d.).
3. James P.C. Southall, *Mirrors, Prisms, and Lenses* (Dover, New York, 1964).
4. *Pinhole Journal*. The Pinhole Resource, Star Route 15, Box 1655, San Lorenzo, NM 88057.
5. Jim Shull, *The Hole Thing A Manual of Pinhole Fotografry* (Morgan, Dobbs Ferry, New York, 1974).
6. M. Young, "Pinhole optics," *Appl. Opt.* **10**, 2763-2767 (1971), and references therein.
7. M. Young, "Pinhole imagery," *Am. J. Phys.* **40**, 715-720 (1972).
8. Matt Young, *Optics and Lasers, Including Fibers and Optical Waveguides*, 3rd ed. (Springer, New York, 1986).
9. John M. Franke, "Field-widened pinhole camera," *Appl. Opt.* **18**, 2913-2914 (1979). See also Tung Hsu, "Reflective wide-angle pinhole camera," *Appl. Opt.* **21**, 2303-2304 (1982).
10. M. Young, "Zone plates and their aberrations," *J. Opt. Soc. Am.* **62**, 972-976 (1972).
11. John W.Y. Lit, "Focussing properties of cascaded apertures," *J. Opt. Soc. Am.* **63**, 491-494 (1972).
12. Adam Lloyd Cohen, "Anti-pinhole imaging," *Optica Acta* **29**, 63-67 (1982).
13. K.D. Möller, *Optics* (University Science Books, Mill Valley, CA, 1988), pp. 161-163.
14. Jearl Walker, "The pleasure of the pinhole camera and its relative the pinspeck camera," *Sci. Am.* **245** (11), 192-200 (1981).
15. A. Zermeno, L.M. Marsh, Jr., and J.M. Hevesi, Imaging by Point Absorption of Radiation, U.S. Patent 4 085 324, 1978.
16. A.T. Young, "Television photometry: the mariner experience," *Icarus* **21**, 262-282 (1974).
17. M. Young, "Quantum noise limits the pinspeck camera to simple objects," *J. Opt. Soc. Am.* **72**, 402-403 (1982).
18. T.H. Nilsson, "Pinhead mirror: a previously undiscovered imaging device?," *Appl. Opt.* **25**, 2863-2864 (1986).
19. Letters, *Lasers and Optronics*, July, 1987, p. 12.