General Relativity HW 3 Quiz

Name_____

You can try both problems below, but you will only receive credit for the most correct solution.

1. (10pts) Given $T_{\mu\nu} = \begin{pmatrix} 1 & 2 & -1 \\ -2 & 1 & 1 \\ -1 & 1 & 1 \end{pmatrix}$ in a space with metric $g_{\mu\nu} = \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1/2 & 0 \\ 0 & 0 & 1/2 \end{pmatrix}$, determine the components of $T^{[\mu\nu]}$.

2. (10pts) Given
$$F_{\mu\nu}=\begin{pmatrix} 0 & -E_x & -E_y & -E_z \\ E_x & 0 & B_z & -B_y \\ E_y & -B_z & 0 & B_x \\ E_z & B_y & -B_x & 0 \end{pmatrix}$$
 show that $\partial_\mu F^{\nu\mu}=J^\nu$ where $J^\nu=(\rho,J^x,J^y,J^z)$ implies that $\vec{\nabla}\cdot\vec{E}=\rho$.